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First principle of derivative. Derivatives using the first principle. Derivatives first principle rule.